

## CRYPTOGRAPHIC DEVICE

## TECHNICAL FIELD

The present invention relates to an encryption device for concealing data in data communication or storage and, more particularly, to an encryption device of a secret-key algorithm which

5 encrypts or decrypts data in blocks using a secret key.

A typical secret-key algorithm, which is used in an encryption device to conceal data, is the DES (Data Encryption Standard) that is a FIPS-approved algorithm for encryption (FIPS 46-3).

10 Fig. 1 illustrates the functional configuration of the DES. The DES uses a 56-bit secret key to encrypt or decrypt data in blocks of 64 bits. In Fig. 1 the encryption process begins with the initial permutation of 64 bits of a plaintext P in an initial permutation part 11 which is followed by splitting the transformed data into two

15 pieces of 32-bit block data  $L_0$  and  $R_0$ . The block data  $R_0$  is input into a function operation part (which is commonly called a round function) 12 shown as an i-th round processing part 14<sub>i</sub> ( $i=0, 1, \dots, 15$ ) in Fig. 2, wherein it is transformed to  $f(R_0, k_0)$  using a 48-bit extended key  $k_0$ . This transformed data ( $R_0, k_0$ ) and the block data

20  $L_0$  are exclusive ORed in an XOR circuit 13, and its output and the block data  $R_0$  are interchanged to obtain the next block data  $L_1, R_1$ . That is,

$$\begin{aligned} R_1 &= L_0 \oplus F(R_0, k_0) \\ L_1 &= R_0 \end{aligned} \quad (1)$$

25 A 0-th round processing part 14<sub>0</sub> is comprises an operation part 12, an exclusive OR circuit 13 and a data swapping part, by

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which two pieces of input data  $L_0$  and  $R_0$  are subjected to round processing to provide output block data  $L_1$  and  $R_1$ , and similar round processing parts  $14_1$  to  $14_{15}$  are provided in cascade. The processing by the  $i$ -th round processing part  $14_i$  will hereinafter be referred to as  $i$ -th processing, where  $i=0, \dots, 15$ . That is, each round processing part  $14_i$  ( $0 \leq i < 15$ ) performs the following processing

$$\begin{aligned} R_{i+1} &= L_i \oplus f(R_i, k_i) \\ L_{i+1} &= R_i \end{aligned} \quad (2)$$

and finally combines two pieces of data  $R_{16}$  and  $L_{16}$  into 64-bit data, which is transformed in a final permutation part 15 to provide a 64-bit ciphertext. The decryption processing can be performed following the same procedure as that for the encryption processing except inputting extended keys  $k_0, k_1, \dots, k_{14}, k_{15}$  into a function  $f$  in the order  $k_{15}, k_{14}, \dots, k_1, k_0$  which is reverse to that in the encryption processing. In such an instance, the outputs  $L_{16}$  and  $R_{16}$  from the final round processing part  $14_{15}$  are further swapped as depicted, and in the decryption processing the plaintext is provided intact at the output of the final permutation part 15 by inputting the ciphertext into the initial permutation part 11 to subject it to the processing of Fig. 1. Of course, exactly the same result could be obtained even by providing data to the final permutation part 15 without swapping the outputs of the final round processing part  $14_{15}$ . Incidentally, the extended keys  $k_0, k_1, \dots, k_{14}, k_{15}$  are generated by extending a 56-bit secret key to 16 48-bit extended keys with a total of 768 bits in an extended key generation part 16 separate of the encryption processing.

The processing in the function operation part 12 is performed as

shown in Fig. 2. To begin with, the 32-bit block data  $R_1$  is transformed to 48-bit data  $E(R_1)$  in an extended permutation part 17. This output data and the extended key  $k_1$  are exclusive ORed in an XOR circuit 18, whose output is transformed to 48-bit data  $E(R_1) \oplus k_1$ , which is then split to eight pieces of 6-bit sub-block data. The eight pieces of sub-block data are input into different S-boxes  $S_1$  to  $S_8$  to derive therefrom a 4-bit output, respectively. Incidentally, the S-box  $S_j$  ( $j=1, \dots, 8$ ) is a nonlinear transformation table that transforms the 6-bit input data to the 4-bit output data, and this is a part that assumes a key role essentially in providing security for the DES. The eight pieces of output data from the S-boxes  $S_1$  to  $S_8$  are concatenated again to 32-bit data, which is applied to a transpose part 19 to obtain an output  $f(R_1, k_1)$  of the function  $f$  which is exclusive ORed with  $L_1$  as depicted in Fig. 8.

Next, a description will be given of cryptanalysis techniques. A wide variety of cryptanalysis techniques have been proposed for the DES and other traditional secret-key algorithms; extremely effective cryptanalysis techniques among them are a differential cryptanalysis technique proposed by E. Biham and A. Shamir ("Differential Cryptanalysis of DES-like Cryptosystems," Proceedings of CRYPTO'90) and a linear cryptanalysis technique proposed by Matsui (Linear Cryptanalysis (I) of DES Cryptosystem," The 1993 Symposium on Cryptography and Information Security 1993, SCIS93-3C).

With the difference between two pieces of data  $X$  and  $X^*$  defined as

$$\Delta X = X \oplus X^* \quad (3)$$

the differential cryptanalysis aims to obtain the extended key  $k_{15}$  in the final round by applying to the following equations two sets of plaintext-ciphertext pairs that an attacker possesses. Let  $L_i$  and  $R_i$  represent two pieces of block data for a first plaintext input into each round processing part  $14_i$  of Fig. 1 and  $L^*_i$  and  $R^*_i$  represent two pieces of block data for a second plaintext input into each round processing part  $14_i$ . And let it be assumed that ciphertexts are provided in response to the input of these first and second plaintexts. Under the definition of Eq. (3), it holds that

$$\begin{aligned} \Delta L_i &= L_i \oplus L^*_i \\ \Delta R_i &= R_i \oplus R^*_i \end{aligned} \quad (4)$$

In Fig. 1, since  $L_{15} = R_{14}$ ,  $L^*_{15} = R^*_{14}$ ,  $L_{16} = R_{15}$  and  $L^*_{16} = R^*_{15}$ , the following equations hold

$$\begin{aligned} R_{16} &= L_{15} \oplus f(R_{15}, k_{15}) \\ R^*_{16} &= L^*_{15} \oplus f(R^*_{15}, k_{15}) \end{aligned} \quad (5)$$

and the exclusive OR of both sides of these two equations is obtained as follows:

$$\Delta R_{16} = \Delta L_{15} \oplus f(L_{16}, k_{15}) \oplus f(L_{16} \oplus \Delta L_{16}, k_{15}) \quad (6)$$

The exclusive ORing of its both sides with  $\Delta R_{14} = \Delta L_{15}$  gives the following equation:

$$f(L_{16}, k_{15}) \oplus f((L_{16} \oplus \Delta L_{16}), k_{15}) = \Delta R_{16} \oplus \Delta R_{14} \quad (7)$$

At this time,  $L_{16}$ ,  $\Delta L_{16}$  and  $\Delta R_{16}$  are data available from the ciphertext, and hence they are known information. Hence, if the attacker can correctly obtain  $\Delta R_{14}$ , then only  $k_{15}$  in the above equation becomes an unknown constant; the attacker can find a correct  $k_{15}$  without fail by making an exhaustive search for  $k_{15}$  through utilization of the known sets of plaintext-ciphertext pairs.

On the other hand,  $\Delta R_{14}$  is difficult in general to obtain since this value is an intermediate difference value. Then, assume that the each round processing part  $14_i$  are approximated by the following equations with a probability  $p_i$  in each of the 0-th to the last round but one:

$$\begin{aligned}\Delta R_{i+1} &= \Delta L_i \oplus \Delta\{f(\Delta R_i)\} \\ \Delta L_{i+1} &= \Delta R_{i+1}\end{aligned}\quad (8)$$

The point is that when certain  $\Delta R_i$  is input,  $\Delta\{f(\Delta R_i)\}$  can be predicted with the probability  $p_i$  regardless of the value of the extended key  $k_i$ . The reason for which such approximations can be made is that  $\Delta\{f(\Delta R_i)\}$  is affected only by the S-box part which is a nonlinear transformation table, and that according to the input differences thereto, the S-boxes provide an extremely uneven distribution of difference outputs. For example, in the S-box S1, an input difference "110100" is transformed to an output difference "0010" with a probability of 1/4. Then, the approximation for each round is obtained by assuming that each S-box is capable of predicting the relationship between the input difference and the output difference with a probability of  $p_{si}$  and by combining them. Furthermore, the concatenation of such approximations in the respective rounds makes it possible to obtain  $\Delta R_{14}$  from  $\Delta L_0$  and  $\Delta R_0$  ( $\Delta L_0$  and  $\Delta R_0$  are data derivable from the plaintext, and hence they are known.) with a probability of  $P = \prod p_i$ . Incidentally, the higher the probability  $P$ , the easier the cryptanalysis. After the extended key  $k_{15}$  is thus obtained, a similar calculation is made of the extended key  $k_{14}$  regarding it as a 15-round DES that is one round fewer than in the above; such operations are repeated to obtain the extended keys one

by one to  $k_0$ .

Biham et al. say that the DES could be broken by this cryptanalysis if  $2^{47}$  sets of chosen plaintext-ciphertext pairs are available.

5       The linear cryptanalysis aims to obtain extended keys by constructing the following linear approximate expression and using the maximum likelihood method with sets of known plaintext-ciphertext pairs to the attacker.

$$\begin{aligned} & (L_0, R_0) \cdot \Gamma(L_0, R_0) \oplus (L_{16}, R_{16}) \cdot \Gamma(L_{16}, R_{16}) \\ 10 \quad & = (k_0, k_1, \dots, k_{15}) \cdot \Gamma(k_0, k_1, \dots, k_{15}) \end{aligned} \quad (9)$$

where  $\Gamma(X)$  represents the vector that chooses a particular bit position of  $X$ , and it is called a mask value.

15       The role of the linear approximate expression is to approximately replace the cryptographic algorithm with a linear expression and separate it into a part concerning the set of plaintext and ciphertext and a part concerning the extended key. That is, in the set of plaintext-ciphertext pair, the exclusive ORs between the values at particular bit positions of the plaintext and those of the ciphertext all take a fixed value, which indicates that it equals the  
20       exclusive OR of the values at particular bit positions of extended keys. This means that the attacker gets information

$$(k_0, k_1, \dots, k_{15}) \cdot \Gamma(k_0, k_1, \dots, k_{15}) \quad (1 \text{ bit})$$

from information

$$(L_0, R_0) \cdot \Gamma(L_0, R_0) \oplus (L_{16}, R_{16}) \cdot \Gamma(L_{16}, R_{16}).$$

25       At this time,  $(L_0, R_0)$  and  $(L_{16}, R_{16})$  are the plaintext and the ciphertext, and hence they are known. For this reason, if the attacker can correctly obtain  $\Gamma(L_0, R_0)$ ,  $\Gamma(L_{16}, R_{16})$  and  $\Gamma(k_0, k_1, \dots,$

$k_{15}$ ), then he can obtain  $(k_0, k_1, \dots, k_{15}) \cdot \Gamma(k_0, k_1, \dots, k_{15})$  (1 bit).

In the DES, it is only in the S-box that the nonlinear transformation is performed; hence, if only the S-box can be linearly represented, the linear approximate expression can easily be constructed. Then, assume that each S-box  $S_i$  can be linearly represented with a probability of  $p_{si}$ . The point here is that when the input mask value for the S-box is given, its output mask value can be predicted with the probability of  $p_{si}$ . The reason for this is that the S-boxes, which form a nonlinear transformation table, provide an extremely uneven distribution of difference mask values according to the input mask values. For example, in the S-box  $S_5$ , when the input mask value is "010000," an output mask value "1111" is predicted with a probability of  $3/16$ . By combining mask values in these S-boxes, a linear approximation can be made in each round between the input mask value and the output mask value with a probability  $p_i$ , and by concatenating the linear approximations in the respective rounds,  $\Gamma(L_0, R_0)$ ,  $\Gamma(L_{16}, R_{16})$  and  $\Gamma(k_0, k_1, \dots, K_{15})$  are obtained with the following probability:

$$P = 2^{n-1} \prod p_i - 1/2 \quad (10)$$

Here, the higher the probability  $P$ , the easier the cryptanalysis.

According to Matsui, he has succeeded in the analysis of the DES by this cryptanalysis through utilization of  $2^{43}$  sets of known plaintext-ciphertext pairs.

To compete against the above cryptanalysis techniques, the probability  $P$  needs only to be reduced to a sufficiently low. Accordingly, a wide variety of proposals have been made to lessen the probability  $P$ , and the easiest way to provide increased security

in the conventional cryptosystem is to increase the number of rounds. For example, a Triple-DES formed by a concatenation of three DESs essentially increases the number of rounds from 16 to 48, and it provides a far lower probability  $P$  than in the case of the DES.

5        However, to increase the number of rounds with a view to competing against the cryptanalysis techniques described above inevitably enlarges the scale of the cryptographic device used and increases the amount of data to process as well. For example, if the number of rounds is tripled, the workload for encryption will also  
10       increase threefold. That is, since the encryption speed of the present DES is about 10 Mbps in the Pentium PC class, the encryption speed of the Triple-DES goes down to around 3.5 Mbps. On the other hand, networks and computers are becoming increasingly faster year by year, and hence there is also a demand for encryption devices that  
15       keep up with such speedups. With conventional cryptographic devices, it is extremely difficult, therefore, to simultaneously meet the requirements of speedup and security.

      The present invention is intended to obviate the abovesaid defects of the prior art and has for its object to provide a  
20       cryptographic device that satisfies the security requirement without increasing the number of rounds.

#### DISCLOSURE OF THE INVENTION

      The present invention is characterized in that a nonlinear  
25       function part, in particular, is provided with: a key-dependent linear transformation part which linearly transforms input data of the nonlinear function part based on key data stored in a key storage

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part; a splitting part which splits the output data of the key-dependent linear transformation part to a plurality of bits strings; first nonlinear transformation parts which nonlinearly transform these split bit strings, respectively; a first linear transformation part which linearly transforms the respective output bits strings of the first nonlinear transformation parts in association with each other; second nonlinear transformation parts which nonlinearly transform some or all of the output bit strings of the first linear transformation part; and a combining part which combines the output bit strings of the second nonlinear transformation parts into output data of the nonlinear function part.

To provide increased security, the invention is characterized by a second linear transformation part which linearly transforms the output data of the combining part to the output data of the nonlinear function part.

Furthermore, the invention is characterized in that either one or both of the first and second linear transformation parts are key-dependent linear transformation parts which linearly transform the input data thereto based on key data stored in the key storage part.

According to the present invention, it is guaranteed that when the probability in the S-boxes is  $p_{si} \leq p_b < 1$  (where  $p_b$  is the maximum differential or linear probability in the S-boxes), the probability of approximating each round is  $p_i \leq p_b^2$  (when the input difference to the function  $f$  is not 0 in the case of the differential cryptanalysis, and when the output mask value from the function  $f$  is not 0 in the case of the linear cryptanalysis). And when the function  $f$  is bijective (in which case a different input always

provides a different output), if the number of rounds of the cipher is set at  $3m$ , then the probability of the cipher becomes  $P \leq p_i^{2m} \leq p_b^{4m}$ . In general, cipher are regarded as being secure against the differential and linear cryptanalysis schemes if  $P < 2^{-64}$ ; hence, it is necessary only to satisfy  $m > -16/\{\log_2(p_b)\}$ , and if  $p_b \leq 2^{-4}$ , it is possible to ensure security with a smaller number of rounds than 16 rounds needed in the DES. The probability of security changes for each multiple of  $m$  rounds.

The present invention ensures security against the differential and linear cryptanalysis with a relatively small number of rounds, and hence it permits implementation of a cryptographic device which copes with both security and low workload.

#### BRIEF DESCRIPTION OF THE DRAWINGS

Fig. 1 is diagram depicting the functional configuration of a conventional DES cryptographic device.

Fig. 2 is a diagram depicting a concrete functional configuration of an  $f$ -functional calculus part 12 in Fig. 1.

Fig. 3 is a diagram illustrating the functional configuration of Embodiment 1 of the present invention.

Fig. 4 is a diagram showing in detail an example of the functional configuration of a nonlinear function part 304 in Embodiment 1.

Fig. 5 is a diagram depicting a concrete example of a key-dependent linear transformation part 347 in Fig. 4.

Fig. 6 is a diagram illustrating the functional configuration of Embodiment 2 of the present invention.

Fig. 7A is a diagram showing in detail the functional configuration of a nonlinear function part 304 in Embodiment 2.

Fig. 7B is a diagram showing a concrete example of a linear transformation part 354 in the nonlinear function part 304.

5 Fig. 8 is a diagram illustrating the functional configuration of Embodiment 3 of the present invention.

Fig. 9 is a diagram showing in detail the functional configuration of a nonlinear function part 304 in Embodiment 3.

10 BEST MODE FOR CARRYING OUT THE INVENTION  
EMBODIMENT 1

An embodiment of the present invention will be described below with reference to the accompanying drawings.

15 Fig. 3 depicts the functional configuration for an encryption procedure in the cryptographic device according to an embodiment of the present invention. The cryptographic device of the present invention also splits input data to two pieces of block data  $L_0$  and  $R_0$  and subjects them to round processing by  $n$  cascade-connected round processing parts  $38_0$  to  $38_{n-1}$  in a sequential order; each  
20 round processing part  $38_i$  ( $i=0, 1, \dots, n-1$ ) is made up of a nonlinear function part 304 corresponding to the round function part 12 in Fig. 1, a linear operation part 305 corresponding to the XOR circuit 13 in Fig. 1 and a swapping part 306.

25 Input data  $P$ , which corresponds to a plaintext, is entered into the cryptographic device via an input part 301. The following key data is generated in advance by an extended key generation part 321 on the basis of the data input thereto from a key input part 320 and

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stored in a key storage part 322.

$\{fk; k_{00}, k_{10}, k_{20}; k_{01}, k_{11}, k_{21}; \dots; k_{0(n-1)}, k_{1(n-1)}, k_{2(n-1)}; ek\}$

The input plaintext data P is transformed in a key-dependent initial linear transformation part 302 with the extend key fk stored in the key storage part 322, thereafter being split in an initial splitting part 303 to two pieces of block data  $L_0$  and  $R_0$ . For example, 64-bit data is split to two pieces of 32-bit block data  $L_0$  and  $R_0$ . The block data  $R_0$  is input to the nonlinear function part 304 of the 0-th round processing part  $38_0$ , together with the extended key  $k_{00}, k_{10}$  and  $k_{20}$  stored in the key storage part 322, and in the nonlinear function part it is transformed to data  $Y_0$ . The data  $Y_0$  and the block data  $L_0$  are transformed to data  $L_0^*$  through an operation in the linear operation part 305. The data  $L_0^*$  and the block data  $R_0$  are subjected to data-position swapping in the swapping part 306 to provide  $L_1 = R_0$  and  $R_1 = L_0^*$ ;  $L_1$  and  $R_1$  are fed to the next first round processing part  $38_1$ .

Thereafter, in an  $i$ -th round processing part  $38_i$  ( $i=1, \dots, n-1$ ) the same processing as described above is repeated for two pieces of block data  $L_i$  and  $R_i$ . That is, in the  $i$ -th round processing part  $38_i$  the data  $R_i$ , one of the two pieces of block data  $L_i$  and  $R_i$ , is input into the nonlinear function part 304, together with the extended key  $k_{0i}, k_{1i}$  and  $k_{2i}$  stored in the key storage part 322, and in the nonlinear function part 304 it is transformed to data  $Y_i$ . The data  $Y_i$  and the block data  $L_i$  are transformed to data  $L_i^*$  by an operation in the linear operation part 305. The data  $L_i^*$  and the data  $R_i$  are swapped in data position in the swapping part 306 to  $L_{i+1} = R_i$  and  $R_{i+1} = L_i^*$ . The linear operation part 305 is one that performs, for

instance, an exclusive-OR operation.

Letting  $n$  represent the repeat count suitable to ensure security of the cryptosystem, two pieces of data  $L_n$  and  $R_n$  are obtained as the result of such repeated processing by the round processing parts  $38_0$  to  $38_{n-1}$ . These pieces of data  $L_n$  and  $R_n$  are combined into a single piece of block data in a final combining part 307; for example, two pieces of 32-bit data  $L_n$  and  $R_n$  are combined to 64-bit data. Then the thus combined data is transformed in a key-dependent final linear transformation part 308 using the extended key  $ek$  stored in the key storage part 322, and output data  $C$  is provided as a ciphertext from an output part 309.

To decrypt, the encryption procedure needs only to be reversed, by which the plaintext  $P$  can be derived from the ciphertext  $C$ . This can be done, for example, by inputting ciphertext data in place of the input data in Fig. 3 and then inputting the extended key in a sequential order reverse to that in Fig. 3, that is,  $ek, k_{0(n-1)}, k_{1(n-1)}, k_{2(n-1)}, \dots, k_{01}, k_{11}, k_{21}, k_{00}, k_{10}, k_{21}, f_k$ .

Fig. 4 illustrates the functional configuration of the nonlinear function part 304 used in each round processing part  $38_i$ . The block data  $R_i$  to the  $i$ -th round processing part  $38_i$  constitutes input data to the nonlinear function part 304, together with the extended key  $k_{0i}, k_{1i}$  and  $k_{2i}$  stored in the key storage part 322. The block data  $R_i$  is linearly transformed to data  $R_i^*$  in a key-dependent linear transformation part 341 using the extended key  $k_{0i}$ . The data  $R_i^*$  is splitting, for instance, to four pieces of 8-bit data  $in_0, in_1, in_2$  and  $in_3$  in a splitting part 342. The four pieces of data  $in_0, in_1, in_2$  and  $in_3$  are nonlinearly transformed to four pieces of data  $mid_{00}, mid_{01},$

$mid_{02}$  and  $mid_{03}$  in nonlinear transformation parts 343, 344, 345 and 346, respectively, from which they are input to a key-dependent linear transformation part 347.

The key-dependent linear transformation part 347 is made up of four processing routes  $30_0$  to  $30_3$  each of which contains at least one exclusive OR circuit as depicted in Fig. 5; these processing routes are logically combined by those exclusive OR circuits. Each processing route performs a linear operation (an exclusive-OR operation) of its own data with those of the other processing routes to generate uniformed pieces of data in the respective processing routes; in the example of Fig. 5, they are further linearly processed by extended key  $k_{1i}$ . That is, the pieces of data  $mid_{00}$ ,  $mid_{01}$ ,  $mid_{02}$  and  $mid_{03}$  are fed into the processing routes  $30_0$  to  $30_3$ , respectively. In the processing route  $30_1$  the pieces of input data  $mid_{00}$  and  $mid_{01}$  are exclusive ORed by an XOR  $31_1$ , and in the processing route  $30_2$  the pieces of input data  $mid_{02}$  and  $mid_{03}$  are exclusive ORed by an XOR  $31_2$ , and the outputs from the XOR  $31_1$  and the XOR  $31_2$  are exclusive ORed by an XOR  $32_2$ . The outputs from the XOR  $31_1$  and the XOR  $32_2$  are exclusive ORed by an XOR  $33_1$ , then the output from the XOR  $33_1$  and the input data  $mid_{00}$  are exclusive ORed by an XOR  $34_0$ , and the output from the XOR  $32_2$  and the input data  $mid_{03}$  are exclusive ORed by an XOR  $34_3$ . Furthermore, the outputs from the XORs  $34_0$ ,  $33_1$ ,  $32_2$  and  $34_3$  and extended key  $k_{1i0}$ ,  $k_{1i1}$ ,  $k_{1i2}$  and  $k_{1i3}$  are exclusive ORed by XORs  $35_0$  to  $35_3$ , from which  $mid_{10}$ ,  $mid_{11}$ ,  $mid_{01}$  and  $mid_{13}$  are output, respectively. That is, the input data  $mid_{00}$ ,  $mid_{01}$ ,  $mid_{02}$  and  $mid_{03}$  to the processing routes  $30_0$  to  $30_3$  are associated with one another and then undergo linear

transformations which are dependent on the key data  $k_{1i0}$ ,  $k_{1i1}$ ,  $k_{1i2}$  and  $k_{1i3}$ , respectively. In short, logical operations given by the following logical expressions are performed.

$$\text{mid}_{10} = \text{mid}_{00} \oplus \text{mid}_{02} \oplus \text{mid}_{03} \oplus k_{1i0}$$

5  $\text{mid}_{11} = \text{mid}_{02} \oplus \text{mid}_{03} \oplus k_{1i1}$

$$\text{mid}_{12} = \text{mid}_{00} \oplus \text{mid}_{01} \oplus \text{mid}_{02} \oplus \text{mid}_{03} \oplus k_{1i2}$$

$$\text{mid}_{13} = \text{mid}_{00} \oplus \text{mid}_{01} \oplus \text{mid}_{02} \oplus k_{1i3} \quad (11)$$

As is evident from these expressions, the output from each processing route of the key-dependent linear transformation part <sup>347</sup>34 contains input data of at least two or more other routes in the form of exclusive ORs in this example, and accordingly the output data of each route is so uniformed as to contain two or more components of the four pieces of input data.

These pieces of output data  $\text{mid}_{10}$ ,  $\text{mid}_{11}$ ,  $\text{mid}_{12}$  and  $\text{mid}_{13}$  are nonlinearly transformed to corresponding pieces of data  $\text{out}_0$ ,  $\text{out}_1$ ,  $\text{out}_2$  and  $\text{out}_3$  in nonlinear transformation parts 348, 349, 350 and 351, respectively, and the pieces of data are provided as output data from the respective processing routes to a combining part 352, wherein they are combined into a single piece of block data  $Y_i^*$ .

That is, for example, four pieces of 8-bit data are combined into one piece of 32-bit data. The data  $Y_i^*$  is linearly transformed by extended key  $k_{2i}$  to data  $Y_i$  in a key-dependent linear transformation part 353; thus, the output data  $Y_i$  from the nonlinear function part 304 is generated. The nonlinear transformation parts 343 to 346 and 348 to 351 are similar, for instance, to the S-box in the DES, and they are each formed, for example, by a ROM whose output data differs with the input data thereto.

The four nonlinear transformation parts 343 to 346 are arranged in parallel and their transformation processes are not associated with one another, and hence they can be executed in parallel; accordingly, an increase in the processing time by

5 increasing the number of such nonlinear transformation parts can be deal with by the parallel processing thereof. The same is true of the nonlinear transformation parts 348 to 351.

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The time necessary for processing in the linear operation part 305 (Fig. 3) and the key-dependent linear transformation parts 341, 10 347 and 353 (Fig. 4), which constitute each round processing part 38<sub>i</sub>, is appreciably shorter than the time required to perform processing of the nonlinear transformation parts 343 to 345 and 348 to 351 similar to the S-box; therefore, the time necessary for encryption processing is substantially in proportion to the number of 15 S-boxes or nonlinear transformation parts used. However, since the key-dependent linear transformation part 347 renders plural pieces of input data into uniformed outputs as described previously, it is possible to omit one or more of the nonlinear transformation parts 348 to 351 and input the corresponding pieces of data into the 20 combining part 352 when it is preknown that the key-dependent linear transformation part 347 performs such a particular linear transformation as described above with reference to Fig. 5. This can be done without diminishing the security against the differential and linear cryptanalysis, and the workload for encryption can be 25 reduced by the number of nonlinear transformation parts thus omitted. For example, when the key-dependent linear transformation part 347 is such as shown in Fig. 5, even if the



nonlinear transformation parts 349 and 350 are omitted and the pieces of data  $mid_{11}$  and  $mid_{12}$  are fed intact into the combining part 352, the security against the differential and linear cryptanalysis remains unchanged but the encryption speed increases about 33%.

5 In other words, when the operation of the key-dependent linear transformation part 347 is predetermined, the presence of one or more of the nonlinear transformation parts 348 to 351 may sometimes has nothing to do with the security against the differential and linear cryptanalysis, in which case they can be  
10 omitted.

Incidentally, in Fig. 3 the generation of the extended key  $\{fk, k_{00}, k_{10}, k_{20}, k_{01}, k_{11}, \dots, k_{0(n-1)}, k_{1(n-1)}, k_{2(n-1)}, ek\}$  by the extended key generation part 321 can be done in the same manner as in the extended key generating part 16 for the DES in Fig. 1.

15 If the above cryptographic device is designed so that, for example, the nonlinear transformation parts 343 to 346 and 348 to 351 are each approximated with a probability of  $p_b = 2^{-6}$  by the differential and linear cryptanalysis techniques and that each round processing part 38<sub>i</sub> performs the nonlinear transformation twice,  
20 that is, performs in tandem the processing by the transformation parts 343 to 346 and the processing by the transformation parts 348 to 351, each round is approximated with a probability of  $p_i \leq 2^{-12}$ ; setting the number  $n$  of rounds at  $n = 3m$ , the round processing of the entire cryptographic device is approximated with a probability  
25 of  $P \leq 2^{-24m}$ . For example, if  $m = 4$  (the number of rounds: 12), the probability becomes  $P \leq 2^{-96}$ , which satisfies a security condition  $P < 2^{-64}$  with a smaller number of rounds than that 16 of the DES,

providing a cryptographic device with a sufficiently high level of security against the differential and linear cryptanalysis. That is, according to the present invention, the security against cryptanalysis can be increased by configuring the round function 12 (Fig. 1) to perform the nonlinear transformation twice in succession.

Since the key-dependent initial linear transformation part 302, the key-dependent final linear transformation part 308 and the key-dependent linear transformation parts 347 and 353 are linear transformation parts that are dependent on extended keys, they provide sufficient security against other cryptanalysis as well as the differential and linear cryptanalysis, ensuring the implementation of a cryptographic device that attaches prime importance on security.

The present invention is not limited specifically to this embodiment; for example, if it is desirable to speed up encryption, it is possible to omit any one or all of these key-dependent initial linear transformation part 302, the key-dependent final linear transformation part 308 and the key-dependent linear transformation part 353 as in the embodiment described later on. In this instance, the security against the differential and linear cryptanalysis will not be diminished on the one hand, but on the other hand the processing speed for encryption can be increased corresponding to the number of operations omitted. But there is a fear of providing decreased security against the other cryptanalysis. Alternatively, any one or all of the key-dependent initial linear transformation part 302, the key-dependent final transformation part 308 and the key-dependent linear transformation parts 347 and 353 may be modified to key-independent linear transformation

parts. This will not diminish the security against the other cryptanalysis as well as the differential and linear cryptanalysis, and makes it possible to increase the processing speed for encryption by implement optimization. The linear transformation parts each perform a transposition of swapping bit positions of input data in a predetermined relationship, a rotation of the input data by a predetermined number of bits, and so forth. The key-dependent linear transformation parts each perform a rotation by the number of bits corresponding to the extended key, an exclusive OR of the input data and the extended key, and so on.

#### EMBODIMENT 2

Fig. 6 illustrates an embodiment which omits middle two of the second four nonlinear transformation parts 348 to 351 in the nonlinear function part 304 (Fig. 4) of the first embodiment shown in Fig. 3. In this embodiment there are also omitted the key-dependent initial linear transformation part 302 and the key-dependent final linear transformation part 308.

The input data P equivalent to a plaintext is input into the cryptographic device via the input part 301. The input data P is split to two pieces of block data  $L_0$  and  $R_0$  in the initial splitting part 303. The block data  $R_0$  is input to the nonlinear function part 304 of the 0-th round processing part 38<sub>0</sub>, together with the extended key  $k_{00}$  and  $k_{20}$  stored in the key storage part 322, wherein it is transformed to data  $Y_0$  through transformation processing. The data  $Y_0$  and the data  $L_0$  are transformed to data  $L_0^*$  by an operation in the linear operation part 305. The data  $L_0^*$  and the data  $R_0$  are

subjected to data-position swapping in the swapping part 306 to provide  $L_1 = R_0$  and  $R_1 = L_0^*$ . Thereafter, in the  $i$ -th round processing part 38<sub>*i*</sub> ( $i=1, \dots, n-1$ ) the same processing as described above is repeated for the two pieces of data  $L_i$  and  $R_i$ . That is, the data  $R_i$ , one of the two pieces of data  $L_i$  and  $R_i$ , is input into the nonlinear function part 304, together with the extended key  $k_{0i}$  and  $k_{2i}$  stored in the key storage part 322, and in the nonlinear function part 304 it is transformed to data  $Y_i$ . The data  $Y_i$  and the data  $L_i$  are transformed to data  $L_i^*$  by an operation in the linear operation part 305. The data  $L_i^*$  and the data  $R_i$  are swapped in data position in the swapping part 306 for transformation to  $L_{i+1} = R_i$  and  $R_{i+1} = L_i^*$ .

Letting  $n$  represent the repeat count suitable to ensure security of the cryptosystem, two pieces of data  $L_n$  and  $R_n$  are obtained by such  $n$  repeated rounds of processing. These pieces of data  $L_n$  and  $R_n$  are combined in the final combining part 307, and the combined output is provided to the output part 309, from which the output data  $C$  is output as the ciphertext.

To decrypt, the encryption procedure needs only to be reversed, by which the plaintext  $P$  can be derived from the ciphertext  $C$ .

Fig. 7A illustrates the functional configuration of the nonlinear function part 304 of the  $i$ -th round processing part 38<sub>*i*</sub> in the Fig. 6. The data  $R_i$  from the preceding round processing part constitutes input data to the nonlinear function part 304, together with the extended key  $k_{0i}$  and  $k_{2i}$  stored in the key storage part 322. The data  $R_i$  is linearly transformed to data  $R_i^*$  in the key-dependent linear transformation part 341 using the extended key  $k_{0i}$ . Then the data  $R_i^*$  is split to four pieces of data  $in_0, in_1, in_2$  and  $in_3$  in the

splitting part 342. The four pieces of data  $in_0$ ,  $in_1$ ,  $in_2$  and  $in_3$  are nonlinearly transformed to four pieces of data  $mid_{00}$ ,  $mid_{01}$ ,  $mid_{02}$  and  $mid_{03}$  in the nonlinear transformation parts 343, 344, 345 and 346, respectively, from which they are input to a linear transformation part 354. In the linear transformation part 354 the four pieces of input data are transformed so that they are mutually associated between the four processing routes  $30_0$  to  $30_3$  as depicted in Fig. 7B. This is the same example as in the case of omitting the logical operation with the extended key in Fig. 5 and can be given by the following expressions.

$$\begin{aligned} mid_{10} &= mid_{00} \oplus mid_{02} \oplus mid_{03} \\ mid_{11} &= mid_{02} \oplus mid_{03} \\ mid_{12} &= mid_{00} \oplus mid_{01} \oplus mid_{02} \oplus mid_{03} \\ mid_{13} &= mid_{00} \oplus mid_{01} \oplus mid_{02} \end{aligned} \quad (12)$$

By this linear transformation, uniformed data  $mid_{10}$ ,  $mid_{11}$ ,  $mid_{12}$  and  $mid_{13}$  are generated, and two pieces of data  $mid_{10}$  and  $mid_{13}$  are nonlinearly transformed to data  $out_0$  and  $out_3$  in the nonlinear transformation parts 348 and 351, respectively, after which the four pieces of data  $out_0$ ,  $mid_{11}$ ,  $mid_{12}$  and  $out_3$  are combined into a single piece of data  $Y_i^*$  in the combining part 352. Finally, the data  $Y_i^*$  is linearly transformed to the data  $Y_i$  in the key-dependent linear transformation part 353 using the extended key  $k_{2i}$ , by which the output data  $Y_i$  from the nonlinear function part 304 is generated.

The nonlinear transformation parts 343 to 346 are arranged in parallel and their transformation processes are not associated with one another, and hence they can be executed in parallel. The same

goes for the nonlinear transformation parts 348 and 351. In this embodiment, since the number of second nonlinear transformations in each nonlinear function part 304 is reduced to the outer two (348 and 351) alone, the workload for encryption or decryption can be decreased accordingly.

Incidentally, the extended key  $k_i$  is data transformed in the extended key generation part 321 from the secret key Key input into the cryptographic device via the key input part 320 and stored in the key storage part 322.

In the case of the above cryptographic device, for example, if the nonlinear transformation parts 343 to 346, 348 and 351 are designed to provide an approximate representation with the probability of  $p_b = 2^{-6}$  against the differential and linear cryptanalysis, each round processing part can provide an approximate representation with the same probability of  $p_i \leq 2^{-12}$  as in Embodiment 1; setting the number  $n$  of rounds at  $n = 3m$ , the cryptographic device provides an approximate representation with the probability of  $P \leq 2^{-24m}$  as a whole. For example, if  $m = 4$  (the number of rounds: 12), the probability becomes  $P \leq 2^{-96}$ , ensuring a sufficiently high level of security against the differential and linear cryptanalysis.

Moreover, the presence of the key-dependent linear transformation part 353 provides a margin of security against other cryptanalysis than the differential and linear cryptanalysis, and the simplified configuration as compared with that of Embodiment 1 reduces the workload. That is, the cryptographic device of this embodiment places importance on the balance between security and

reduced workload.

### EMBODIMENT 3

Fig. 8 illustrates an embodiment which omits the key-dependent linear transformation part 353 in the nonlinear function part 304 of the second embodiment depicted in Fig. 6. The input data P equivalent to a plaintext is input into the cryptographic device via the input part 301. The input data P is split to two pieces of block data  $L_0$  and  $R_0$  in the initial splitting part 303. The block data  $R_0$  is input to the nonlinear function part 304 of the 0-th round processing part 38<sub>0</sub>, together with extended key  $k_0$  stored in the key storage part 322, wherein it is transformed to data  $Y_0$  through transformation processing. The data  $Y_0$  and the data  $L_0$  are transformed to data  $L_0^*$  by an operation in the linear operation part 305. The data  $L_0^*$  and the data  $R_0$  are subjected to data-position swapping in the swapping part 306 for transformation to  $L_1 = R_0$  and  $R_1 = L_0^*$ . Thereafter, in the i-th round processing part 38<sub>i</sub> the same processing as described above is repeated for the two pieces of data  $L_i$  and  $R_i$ . That is, the data  $R_i$ , one of the two pieces of data  $L_i$  and  $R_i$ , is input into the nonlinear function part 304, together with extended key  $k_i$  stored in the key storage part 322, and in the nonlinear function part 304 it is transformed to data  $Y_i$ . The data  $Y_i$  and the data  $L_i$  are transformed to data  $L_i^*$  by an operation in the linear operation part 305. The data  $L_i^*$  and the data  $R_i$  are swapped in data position in the swapping part 306 for transformation to  $L_{i+1} = R_i$  and  $R_{i+1} = L_i^*$ , and two pieces of block data  $L_{i+1}$  and  $R_{i+1}$  are output.

Letting  $n$  represent the repeat count suitable to ensure security of the cryptosystem, two pieces of data  $L_n$  and  $R_n$  are obtained by such  $n$  repeated rounds of processing. These pieces of data  $L_n$  and  $R_n$  are combined in the final combining part 307, and the combined output is provided to the output part 309, from which the output data  $C$  is output as the ciphertext.

The ciphertext  $C$  can be deciphered to the plaintext  $P$  by following the encryption procedure in reverse.

Fig. 9 illustrates the functional configuration of the nonlinear function part 304 in the Fig. 8. The data  $R_i$  to the nonlinear function part 304 is fed to the key-dependent linear transformation part 341, together with the extended key  $k_i$  stored in the key storage part 322. The data  $R_i$  is linearly transformed to data  $R_i^*$  in the key-dependent linear transformation part 341 using the extended key  $k_i$ . Then the data  $R_i^*$  is split to four pieces of data  $in_0, in_1, in_2$  and  $in_3$  in the splitting part 342. The four pieces of data  $in_0, in_1, in_2$  and  $in_3$  are nonlinearly transformed to four pieces of data  $mid_{00}, mid_{01}, mid_{02}$  and  $mid_{03}$  in the nonlinear transformation parts 343, 344, 345 and 346, respectively, from which they are input to the linear transformation part 354. The linear transformation part 354 linearly transforms them to the following pieces of data  $mid_{10}, mid_{11}, mid_{12}$  and  $mid_{13}$ , for example, in the same manner as described above with reference to Fig. 7B in Embodiment 2.

$$mid_{10} = mid_{00} \oplus mid_{02} \oplus mid_{03}$$

$$mid_{11} = mid_{02} \oplus mid_{03}$$

$$mid_{12} = mid_{00} \oplus mid_{01} \oplus mid_{02} \oplus mid_{03}$$

$$mid_{13} = mid_{00} \oplus mid_{01} \oplus mid_{02} \quad (13)$$



Then the two pieces of data  $mid_{10}$  and  $mid_{13}$  are nonlinearly transformed to data  $out_0$  and  $out_3$  in the nonlinear transformation parts 348 and 351, respectively, after which the four pieces of data  $out_0$ ,  $mid_{11}$ ,  $mid_{12}$  and  $out_3$  are combined into a single piece of data in the combining part 352, by which the output data  $Y_i$  from the nonlinear function part 304 is generated.

The nonlinear transformation parts 343 to 346 are arranged in parallel and their transformation processes are not associated with one another, and hence they can be executed in parallel. The same goes for the nonlinear transformation parts 348 and 351.

Incidentally, the extended key  $k_i$  is data transformed in the extended key generation part 321 from the secret key Key input into the cryptographic device via the key input part 320 and stored in the key storage part 322.

In the case of the above cryptographic device, for example, if the nonlinear transformation parts 343 to 346, 348 and 351 are designed to provide an approximate representation with the probability of  $p_b = 2^{-6}$  against the differential and linear cryptanalysis, each round processing part can provide an approximate representation with the probability of  $p_i \leq 2^{-12}$ ; setting the number  $n$  of rounds at  $n = 3m$ , the cryptographic device provides an approximate representation with the probability of  $P \leq 2^{-24m}$  as a whole. For example, if  $m = 4$  (the number of rounds: 12), the probability becomes  $P \leq 2^{-96}$ , ensuring a sufficiently high level of security against the differential and linear cryptanalysis.

Moreover, since the cryptographic device of this embodiment has a configuration that includes the minimum number of parts

required to provide a sufficient level of security against the differential and linear cryptanalysis, the workload is reduced and the encryption or decryption speed is improved accordingly.

5 In the above, the splitting part 342 in the nonlinear function part 304 needs not always to split the input data into four but may also split it to an arbitrary number of pieces. In the case splitting the data into four, the number of second nonlinear transformation parts may be reduced to only two as depicted in Figs. 7A and 9.

10 In the following table there are shown, in comparison with the case of the DES of Figs. 1 and 2, the security level per round, the number of rounds satisfying the security requirement and the workload (the number of steps) necessary therefor in the case of using six nonlinear transformation parts (343 to 346, 348, 351) in the nonlinear function part 304 (a round function) depicted in the  
15 second and third embodiments described above. In the comparison, the embodiments of the present invention used a total of 32 bits for the data to the nonlinear transformation parts 343 to 346 which correspond to the S-boxes of the DES, and hence the data to each nonlinear transformation part was 8-bit; therefore, the size of each  
20 S-box was made 8-bit and consequently, the number of S-boxes was four.

Comparative Table

	No. of S-boxes per round	Security level per round	Required No. of rounds	No. of steps
DES	4	$2^{-6}$	17	68
This invention	6	$2^{-12}$	9	54

As will be seen from this table, the number of S-boxes (the number of nonlinear transformation parts) per round in the present invention is larger than in the DES, but the security level per round in the present invention is twice that of the DES. On this account, the number of rounds required to meet the security requirement is smaller than in the case of DES, and the workload (the number of steps) necessary for providing the security is also smaller.

#### EFFECT OF THE INVENTION

As described above in detail, according to the present invention, the input data is split to plural pieces of data in the nonlinear function part, then these pieces of data are nonlinearly transformed and linearly transformed in association with each other, and at least one part of such linearly transformed data is nonlinearly transformed, by which it is possible to provide a highly secure cryptographic device for concealing data in data communication or storage.